

## ML-enhanced Numerics: From Super-resolution to Neural Operators for Parallel-in-Time Methods

Many models in computational science and engineering are based on time-dependent partial differential equations, e.g., the Navier–Stokes equations governing fluid dynamics. Hence, integration along the time axis arises as an important numerical problem in many domains. While spatial domain decomposition is a well-established parallelization strategy, on its own it will not suffice to provide the massive degree of concurrency required by upcoming exascale systems. Parallel-in-time (PinT) methods provide additional concurrency along the temporal axis and can improve parallel scaling. Classical PinT methods like Parareal rely on a computationally cheap coarse integrator to propagate information forward in time, while a parallelizable expensive fine propagator provides accuracy. Typically, the coarse method is a numerical integrator using lower resolution, reduced order or a simplified model. Recent progress on how to solve differential equations with techniques from machine learning can offer an alternative approach to hand-crafted numerical coarse models.

In this talk, we first explore how super-resolution techniques can enhance low-resolution numerical simulations in the ICON-O ocean model. Our method augments a coarse, mesh-based algorithm with frequent, learned corrections that incorporate the effects of unresolved dynamics, resulting in an effectively submesoscale-resolving simulation.

In the second part, we examine how physics-informed neural operators (PINOs) can improve parallel-in-time methods like Parareal and parallel spectral deferred correction methods (pSDC). We demonstrate that PINO-Parareal converges as fast as a bespoke numerical coarse model but provides better overall speedup than space-time parallelization with a numerical coarse propagator. Using Rayleigh–Bénard convection as a case study, we then show how pSDC can improve scaling, and discuss limitations of applying neural operators in this context.